

TSBB15 Computer Vision Lecture 8 Local invariant features



Image Matching

 KLT tracking and block matching are useful when matching between consecutive frames in a video sequence.



Image Matching

- KLT tracking and block matching are useful when matching between consecutive frames in a video sequence.
- Images are from the same camera
- small changes in scale, rotation and illumination



Image Matching

- KLT tracking and block matching are useful when matching between consecutive frames in a video sequence.
- Images are from the same camera
- small changes in scale, rotation and illumination
- Local invariant features work when these conditions are violated.



Wide-baseline stereo

Problem 1: wide-baseline stereo

 Matching images of the same scene, captured at different positions.





Wide-baseline stereo

- Problem 1: wide-baseline stereo
 - Matching images of the same scene, captured at different positions.





Object instance recognition and pose estimation

- Problem 2: object instance recognition
 - Recognition of 3D objects under partial occlusion.
 - training set
 - test set
 - 6dof pose









Object recognition

• Example: Eddie the embodied



See webpage for details
 <u>http://users.isy.liu.se/cvl/perfo/</u>



• In lecture 2 we discussed how to match across scale and translation. How?



- In lecture 2 we discussed how to match across scale and translation. How?
- Another option is to use interest points e.g. Harris points [Z. Zhang et al. 95].
 - A. Detect interest points
 - B. Cut out image patches around each point
 - C. Matches can now be found by comparing patches+epipolar geometry constraints.



 Correspondences from block matching at Harris points.





• After applying the Epipolar constraint (You will test this in lab 3).







• The epipolar constraint: $\mathbf{x}_1^T \mathbf{F} \mathbf{x}_2 = 0$







- The epipolar constraint: $\mathbf{x}_1^T \mathbf{F} \mathbf{x}_2 = 0$
- x₁ and x₂ are projections of the same 3D point in two views.
- Scene is static, i.e. no motion has taken place (except the change of camera position).
- F can be estimated from 7 or more correspondences. E.g. 8-pt algorithm.



- The epipolar constraint: $\mathbf{x}_1^T \mathbf{F} \mathbf{x}_2 = 0$
- See the compendium, Introduction to Estimation, Representation and Geometry, Klas Nordberg



- Zhang's interest point method. (repeat)
 - A. Detect interest points
 - B. Cut out image patches around each point
 - C. Matches can now be found by comparing patches+epipolar geometry constraints.



• Zhang's method is invariant to translation (and partially to scale).

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = s \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \mathbf{t}$$

 2 degrees-of-freedom (DOF) of invariance (transl. only) (3 if scale is also counted)



• Zhang's method is invariant to translation (and partially to scale).

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = s \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \mathbf{t}$$

- 2 degrees-of-freedom (DOF) of invariance (transl. only) (3 if scale is also counted)
- What about image rotations?
- What about view changes?



- In general, the *local invariant feature approach* can be described as three steps:
 - Detection: Use a *detector* to find a local, canonical frame (coordinate system)



- In general, the *local invariant feature approach* can be described as three steps:
 - Detection: Use a *detector* to find a local, canonical frame (coordinate system)
 - Description: Compute a *descriptor*, by sampling the image in the canonical frame



- In general, the *local invariant feature approach* can be described as three steps:
 - Detection: Use a *detector* to find a local, canonical frame (coordinate system)
 - Description: Compute a *descriptor*, by sampling the image in the canonical frame
 - Matching: Find correspondences, by comparing descriptors from two images



Canonical frame example

Resampling to canonical frame





Geometric invariances

Robustness to view changes





Photometric invariances Robustness to illumination changes







- Geometric invariances can be obtained by choosing a frame that is equivariant to rotations, scalings, and image skews
- Photometric invariances can be obtained by computing the descriptor in a more advanced way than direct sampling.



- The geometric invariances we use make a locally planar assumption.
- They can thus be described using *homographies*.



- Recap: A Homography is a transformation between points x on one plane, and points yon another. (y_1) (x_1) (h_1, h_2, h_3) (x_1)

$$\lambda \begin{pmatrix} y_1 \\ y_2 \\ 1 \end{pmatrix} = \mathbf{H} \begin{pmatrix} x_1 \\ x_2 \\ 1 \end{pmatrix} = \begin{pmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ 1 \end{pmatrix}$$



- Recap: A Homography is a transformation between points x on one plane, and points yon another. (y_1) (x_1) (h_1) h_2 h_3 (x_1)

$$\lambda \begin{pmatrix} y_1 \\ y_2 \\ 1 \end{pmatrix} = \mathbf{H} \begin{pmatrix} x_1 \\ x_2 \\ 1 \end{pmatrix} = \begin{pmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ 1 \end{pmatrix}$$

- **Degrees of freedom**: number of unique elements in **H**.
 - at most 8dof (for plane projective case), as H and kH, $k \in \mathbb{R} \setminus 0$ gives the same output



- A hierarchy of transformations:
 scale+translation (3dof)
 - similarity (4dof) (scale+translation+rotation)
 - affine (6dof)(similarity+skew)
 - plane projective (8dof) (affine+forshortening)





- We can find the canonical frame by using more than one point [Brown&Lowe 02] aka. *interest-point* groups
- We will now give some examples...



 Scale+translation: Useful if we know that there is no rotation. E.g. for a camera mounted in a car, looking at upright pedestrians.





 Similarity: Full invariance in image plane, none outside image plane.
 Useful e.g. for pose estimation.





 Affine: Deals with most common projective distortions. Good if patch size is small relative to distance to patch.





 Plane projective: Full modelling of a plane in 3D. Requires more image measurements, but is better for extreme view angles.





Resampling to canonical frame





- Problems with interest-point groups:
 - Sensitive to missing points:
 If e=P(point-detected|present) then
 P(frame-is-detected|present)=e^N
 where N is number of points in frame.
 - Combinatorics: if K points in image, we have $\binom{N}{K}$ possible canonical frames.
 - We will introduce other ways to find the frame soon.


- Image intensity is approx. linear in radiance (at least before gamma correction)
- E.g. adding a second, identical light source will double the sensor activation, *a*(**x**).

$$a(\mathbf{x}) = \int s(\lambda) r(\lambda, \mathbf{x}) e(\lambda) d\lambda$$

 s-sensor absorption spectrum, r-reflectance spectrum of object, e-emission spectrum of light source (attenuated by the atmosphere)



If illumination changes, image matching fails:

$$\begin{aligned}
I(\mathbf{x}) &= I_0(\mathbf{x})k_1 \\
J(\mathbf{x}) &= I_0(\mathbf{x})k_2 \end{aligned} \Rightarrow \sum_{x \in \Omega} (I(\mathbf{x}) - J(\mathbf{x}))^2 = \text{non-zero}
\end{aligned}$$

• We want a function that is invariant to scalings:

$$\sum_{x \in \Omega} (f(I(\mathbf{x})) - f(J(\mathbf{x})))^2 = \text{small number}$$

• How should we choose *f()*?



 For cameras with non non-linear radiometric response (and e.g. gamma correction), or if two different cameras are used we may use the affine model:

$$I(\mathbf{x}) = I_0(\mathbf{x})k_1 + k_2$$

• How should we choose *f* ? we want:

$$\sum_{x \in \Omega} (f(I(\mathbf{x})) - f(J(\mathbf{x})))^2 = \text{small number}$$



- Mean subtraction, derivatives, and other DC free linear filters remove a constant offset in intensity
- Normalising a patch by e.g. the L₂-norm or the standard deviation, removes scalings of the intensity.
- Affine invariance by combining both:

$$\hat{I}(\mathbf{x}) = (I(\mathbf{x}) - \mu_I) / \sigma_I$$







Local Invariant Features

- There are many examples of features that fit the descriptor+detector paradigm.
- The two most widely used are:
 - SIFT Scale Invariant Feature Transform (Lowe 99)
 - MSER Maximally Stable Extremal Regions (Matas et al. 02)
- We will look at these two in more detail.



SIFT

- Scale Invariant Feature Transform
 [Lowe'99]. In brief:
 - The SIFT detector finds points using Difference-of-Gaussians in a pyramid Gives: position x,y and scale s
 - Rotation is found from a gradient histogram
 - This gives a frame for the SIFT descriptor, which is computed from gradient orientation histograms.



- Scale Space (recap.)
 - The image is extended with an extra dimension for scale/blur:

$$f(x, y, s) = (f_0 * g(s))(x, y)$$

– The blurring kernel g(s) is typically a Gaussian:

$$g(\mathbf{x},s) = \frac{1}{2\pi s} e^{-\mathbf{x}^T \mathbf{x}/2s^2}$$



- Scale Selection [Lindeberg'93]
 - Find a characteristic point (e.g. max) on a function of position and scale:

$$(\hat{\mathbf{x}}, \hat{s}) = rg \max h(f(\mathbf{x}, s))$$

– Example: Maximum of normalised Laplacian:

$$h(f(\mathbf{x},s)) = s^2(f * \nabla^2 g(s))(\mathbf{x})$$







 In SIFT, scale selection is done using difference-of-Gaussians:

$$h(f(\mathbf{x},\sigma)) = (f * (g(\sigma) - g(k\sigma)))(\mathbf{x})$$

- Efficient implementation using pyramids [Lowe'99]
- Sampling in scale space with $\Delta \sigma = 1/\sqrt{2}$









Non-max suppression in (x,y,s)



 Finally we find one or more reference directions using a gradient orientation histogram *h* at the found location in scale

space.





- The SIFT detector gives us a similarity frame. What is this?
 - We now want to convert the image patch at the frame to a 128-byte *descriptor vector*.
 - The purpose of this is to add photometric invariance, and some extra translation and scale robustness.



Compute x- and y-gradients through convolution:

$$\nabla \mathbf{f}(\mathbf{x}) = \begin{bmatrix} (d_x * f)(\mathbf{x}) \\ (d_y * f)(\mathbf{x}) \end{bmatrix}$$

- Rotate gradient map to direction from orient-hist: $\nabla \hat{\mathbf{f}}(\mathbf{x}) = \mathbf{R} \nabla \mathbf{f}(\mathbf{R}^T \mathbf{x})$
- Compute gradient orientation histograms in 4x4 spatial regions:

$$h_{kl} = \sum_{\mathbf{x} \in \text{patch}_l} |\nabla \hat{\mathbf{f}}(\mathbf{x})| w(\mathbf{x} + \mathbf{d}_l) B_k(\tan^{-1} \nabla \hat{\mathbf{f}}(\mathbf{x}))$$



Compute gradient orientation histograms in 4x4 spatial regions :

$$h_{kl} = \sum_{\mathbf{x} \in \text{patch}_l} |\nabla \hat{\mathbf{f}}(\mathbf{x})| w(\mathbf{x} + \mathbf{d}_l) B_k(\tan^{-1} \nabla \hat{\mathbf{f}}(\mathbf{x}))$$

- B_k(x) linear interpolation kernel
 Quadratic is better (Jonsson&Felsberg)
- Subwindows $l \in [1 \dots 16]$ directions $k \in [1 \dots 8]$
- Spatial weight $w(\mathbf{x} + \mathbf{d}_l)$ (Gaussian decay)



 Implementation with source code in both VLfeat and OpenCV.



Note that 4x4 regions are actually used, with 8 orientations -> 128 elements



- Affine illumination invariance by using gradients and normalising descriptor $\hat{\mathbf{h}} = \mathbf{h}/||\mathbf{h}||$
- Some robustness by truncating and normalising again $\hat{\hat{\mathbf{h}}} = \min(t, \hat{\mathbf{h}}) / ||\hat{\mathbf{h}}||$
- The spatial histogramming gives robustness to scale/rotation/translation errors.



- Affine illumination invariance by using gradients and normalising descriptor $\hat{\mathbf{h}} = \mathbf{h}/||\mathbf{h}||$
- Some robustness by truncating and normalising again $\hat{\hat{\mathbf{h}}} = \min(t, \hat{\mathbf{h}}) / ||\hat{\mathbf{h}}||$
- The spatial histogramming gives robustness to scale/rotation/translation errors.
- SIFT is used commercially in many places.
 (The Sony AIBO was an early example.)



- Maximally Stable Extremal Regions
 [Matas et al.'02]
- Consider the set of all possible thresholdings of an image...

[Movie clip]







- Connected regions form segments.
 - Cf. Watershed algorithm (similar idea but different output)
 - Look at stability of a function of segment across image evolution. e.g.

area(component(t))

 MSERs are components that are maximally stable, i.e., have a local minimum of the rate of change: darea(component(t))



- compare: Maximal Stability, Scale Selection
- Stability measure: Range of stable thresholds t₂-t₁ around min is called the margin of the region.



– Two possible thresholdings: $I(\mathbf{x}) < t$, $I(\mathbf{x}) > t$



Input image

64 MSER- (total 272) 64 MSER+ (total 294)

Very fast (using union/find+path compression).
MSER type (+/-) is useful for matching How?



- MSER is invariant to monotonic changes of intensity. i.e. I(x) and f(I(x)) have the same output if $f(x+k) > f(x) \forall k > 0$
- Wide range of sizes obtained without a scale pyramid.
 Better still with a pyramid (Forssén&Lowe ICCV'07)
- Colour objects can be tracked by computing MSERs on the Mahalanobis distance to a colour distribution. (Donoser&Bischof CVPR'06)
- Colour regions by looking at gradients.
 Called MSCR (Forssén CVPR'07)





MSCR







MSCR





Reference directions from extremal points along ellipse-normalized contour.





• Approximating ellipse

– from moments of binary mask $v:\Omega\mapsto\{0,1\}$

$$\begin{split} \mu_{k,l}(v) &= \sum_{x} \sum_{y} x^{k} y^{l} v(x, y) \\ \mathbf{m} &= \frac{1}{\mu_{0,0}} \begin{bmatrix} \mu_{1,0} \\ \mu_{0,1} \end{bmatrix} \quad \mathbf{C} &= \frac{1}{\mu_{0,0}} \begin{bmatrix} \mu_{2,0} & \mu_{1,1} \\ \mu_{1,1} & \mu_{0,2} \end{bmatrix} - \mathbf{m} \mathbf{m}^{T} \\ \mathcal{R}(\mathbf{m}, \mathbf{C}) &= \{ \mathbf{x} : (\mathbf{x} - \mathbf{m})^{T} \mathbf{C}^{-1} (\mathbf{x} - \mathbf{m}) \leq 4 \} \end{split}$$



Normalisation to a circle (axis aligned)
 Compute the eigenfactorisation:

$$\mathbf{C} = \mathbf{R} \mathbf{D} \mathbf{R}^T, \quad \det \mathbf{R} > 0$$

The circle normalisation can now be performed as:

$$\mathbf{x} = \mathbf{A}\hat{\mathbf{x}} + \mathbf{m}$$
, for $\mathbf{A} = 2\mathbf{R}\mathbf{D}^{1/2}$

- $\hat{\mathbf{x}}$ canonical coordinates
- **x** image coordinates



- Ellipse+extrema of distance to centre is just one frame construction option.
- Other (affine covariant) choices:
 - Points of maximum curvature.
 - Bi-tangens.
 - See Obdrzalek&Matas BMVC'02
- Implementation w. source: in both VLfeat and OpenCV



MSER descriptor

• The MSER detector originally used normalized colour patches as descriptor vectors:

$$\begin{split} \hat{I}_r(\mathbf{x}) &= (I_r(\mathbf{x}) - \mu_r) / \sigma_r \\ \hat{I}_g(\mathbf{x}) &= (I_g(\mathbf{x}) - \mu_g) / \sigma_g \\ \hat{I}_b(\mathbf{x}) &= (I_b(\mathbf{x}) - \mu_b) / \sigma_b \end{split}$$

• Nowadays other descriptors, e.g. the SIFT descriptor are used.



Other local invariant features

• SFOP

http://www.ipb.uni-bonn.de/sfop/

- BRISK
 Source Code+description
 http://www.asl.ethz.ch/people/lestefan/personal/BRISK
- FREAK and ORB In OpenCV
- SURF and SIFT in OpenCV nonfree



Binary descriptors

• To save memory and time, many descriptors use local binary patterns:



Image from Alexandre et al. CVPR 2012 10110
 sign of intensity difference has monotonic illumination invariance



Binary descriptors

• To save memory and time, many descriptors use local binary patterns:



E.g. BRIEF (ECCV'10), BRISK (ICCV'11), ORB (ICCV'11), FREAK (CVPR'12)



Deep learning descriptors

Examples:

- DeCAF (ArXiv'13) descriptors
- LIFT (ECCV'16) detector and descriptor

Better matching performance at the price of more expensive computations.



A note on invariance

- Always strive to limit amount of invariance
- Use knowledge on imaging situation,
 - e.g. A car mounted camera may not need rotation invariance for pedestrians.
 - e.g. in a video with smooth illumination changes, affine illumination invariance is not necessary



- The *Local Invariant Feature* method:
- Detection
- Description
- Matching



– For a descriptor *q* in a query image. Which prototype in memory (*p*₁,*p*₂,...,*p*_N) is *most likely* to correspond to the same world object?



- For a descriptor *q* in a query image. Which prototype in memory (*p*₁,*p*₂,...,*p*_N) is *most likely* to correspond to the same world object?
- Assuming additive i.i.d. Gaussian noise on all elements: $p(\mathbf{q}|\mathbf{p}_k) \propto \prod_{l=1}^{D} e^{-.5(p_{kl}-q_l)^2/\sigma^2}$ $\max(J) \Leftrightarrow \min(-\log(J))$ $-\log(p(\mathbf{q}|\mathbf{p}_k)) \propto \sum_{l=1}^{D} (p_{kl}-q_l)^2$



- So, the match with smallest distance is most likely correct, assuming i.i.d. Gaussian noise.
- What about the scalar product for normalised vectors/NCC?



- So, the match with smallest distance is most likely correct, assuming i.i.d. Gaussian noise.
- What about the scalar product for normalised vectors/NCC?

$$||\mathbf{p} - \mathbf{q}||^2 = \mathbf{p}^T \mathbf{p} + \mathbf{q}^T \mathbf{q} - 2\mathbf{p}^T \mathbf{q} = 2(1 - \mathbf{p}^T \mathbf{q})$$

- But are all values identically distributed?
- …are they all independent?



• For binary descriptors (e.g. **BRIEF**) the Hamming distance is used:

s = bitcnt(XOR(P,Q))

• Also makes i.i.d. assumption.



Dense invariant features

- (semi-)dense flow for wide baseline problems can be obtained by matching invariant features
- located at every pixel and
- also at several scales
- e.g. SIFTflow, DSIFT, PHOW, DAISY
- Much more expensive to compute. GPGPU etc. is helpful here.



Summary

- Use local invariant features: when KLT fails
- But use no more invariance than needed
- Photometric and Geometric invariance
- Recognition in three steps: Detection, Description and Matching



Upcoming course events

- Lab 2: Those who have not finished have the option to demonstrate the lab on Feb 16, 13.15-15 in Olympen.
- Next Lecture (15/2 10-12) Biological vision. Voluntary.